basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL
SENIOR CERTIFICATE

GRADE 12

MATHEMATICS P1

NOVEMBER 2022

MARKS: 150

TIME: 3 hours

This question paper consists of 9 pages and 1 information sheet.

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of 10 questions.

2. Answer ALL the questions.

3. Number the answers correctly according to the numbering system used in this question paper.

4. Clearly show ALL calculations, diagrams, graphs, etc. that you have used in determining your answers.

5. Answers only will NOT necessarily be awarded full marks.

6. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.

7. If necessary, round off answers to TWO decimal places, unless stated otherwise.

8. Diagrams are NOT necessarily drawn to scale.

9. An information sheet with formulae is included at the end of the question paper.

10. Write neatly and legibly.

QUESTION 1

1.1   Solve for x:

1.1.1 $(3x - 6)(x + 2) = 0$ (2)

1.1.2 $2x^2 - 6x + 1 = 0$ (correct to TWO decimal places) (3)

1.1.3 $x^2 - 90 > x$ (4)

1.1.4 $x - 7\sqrt{x} = -12$ (4)

1.2   Solve for x and y simultaneously:

$2x - y = 2$

$xy = 4$ (5)

1.3   Show that $2.5^n - 5^{n+1} + 5^{n+2}$ is even for all positive integer values of n. (3)

1.4   Determine the values of x and y if: $\dfrac{3^{y+1}}{32} = \sqrt{96^x}$ (4)

[25]

QUESTION 2

2.1   The first term of a geometric series is 14 and the 6th term is 448.

2.1.1   Calculate the value of the constant ratio, r. (2)

2.1.2   Determine the number of consecutive terms that must be added to the first 6 terms of the series in order to obtain a sum of 114 674. (4)

2.1.3   If the first term of another series is 448 and the 6th term is 14, calculate the sum to infinity of the new series. (3)

2.2   If $\displaystyle\sum_{p=0}^{k}\left(\dfrac{1}{3}p + \dfrac{1}{6}\right) = 20\dfrac{1}{6}$, determine the value of k. (5)

[14]

QUESTION 3

It is given that the general term of a quadratic number pattern is $T_n = n^2 + bn + 9$ and the first term of the first differences is 7.

3.1 Show that $b = 4$. (2)

3.2 Determine the value of the 60th term of this number pattern. (2)

3.3 Determine the general term for the sequence of first differences of the quadratic number pattern. Write your answer in the form $T_p = mp + q$. (3)

3.4 Which TWO consecutive terms in the quadratic number pattern have a first difference of 157? (3)

[10]

QUESTION 4

4.1 Sketched below is the graph of $h(x) = \dfrac{1}{x + p} + q$. The asymptotes of h intersect at $(1 ; 2)$.
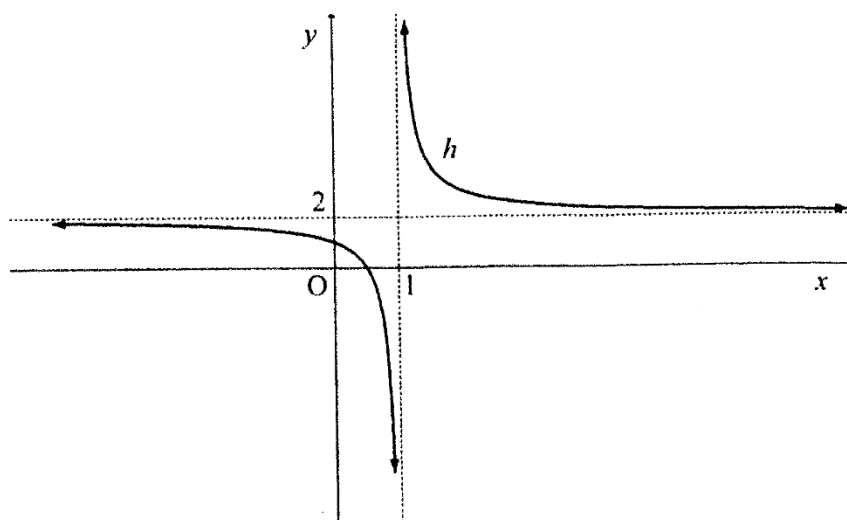
4.1.1 Write down the values of p and q. (2)

4.1.2 Calculate the coordinates of the x-intercept of h. (2)

4.1.3 Write down the x-coordinate of the x-intercept of g if $g(x) = h(x + 3)$. (2)

4.1.4 The equation of an axis of symmetry of h is $y = x + t$. Determine the value of t. (2)

4.1.5 Determine the values of x for which $-2 \le \dfrac{1}{x - 1}$. (3)

4.2 The graphs of $f(x) = x^2 - 4x - 5$ and $g(x) = a.2^x + q$ are sketched below.
- E and H are the x-intercepts of f.
- C is the y-intercept of f and lies on the asymptote of g.
- The two graphs intersect at D, the turning point of f.
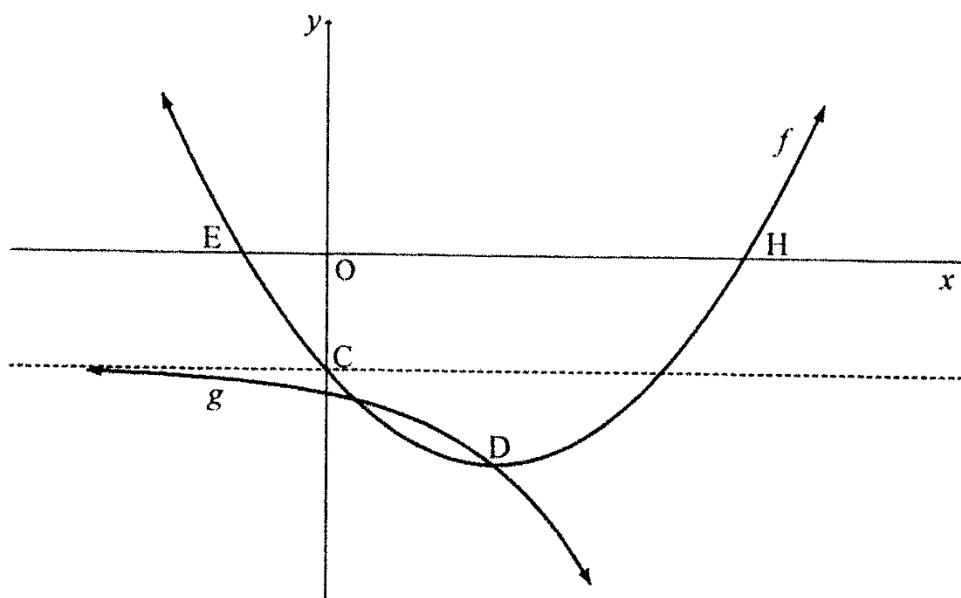
4.2.1	Write down the y-coordinate of C.	(1)
4.2.2	Determine the coordinates of D.	(2)
4.2.3	Determine the values of a and q.	(3)
4.2.4	Write down the range of g.	(1)
4.2.5	Determine the values of k for which the value of $f(x) - k$ will always be positive.	(2)

[20]

QUESTION 5

The graphs of $g(x) = 2x + 6$ and g^{-1}, the inverse of g, are shown in the diagram below.

- D and B are the x- and y-intercepts respectively of g.
- C is the x-intercept of g^{-1}.
- The graphs of g and g^{-1} intersect at A.
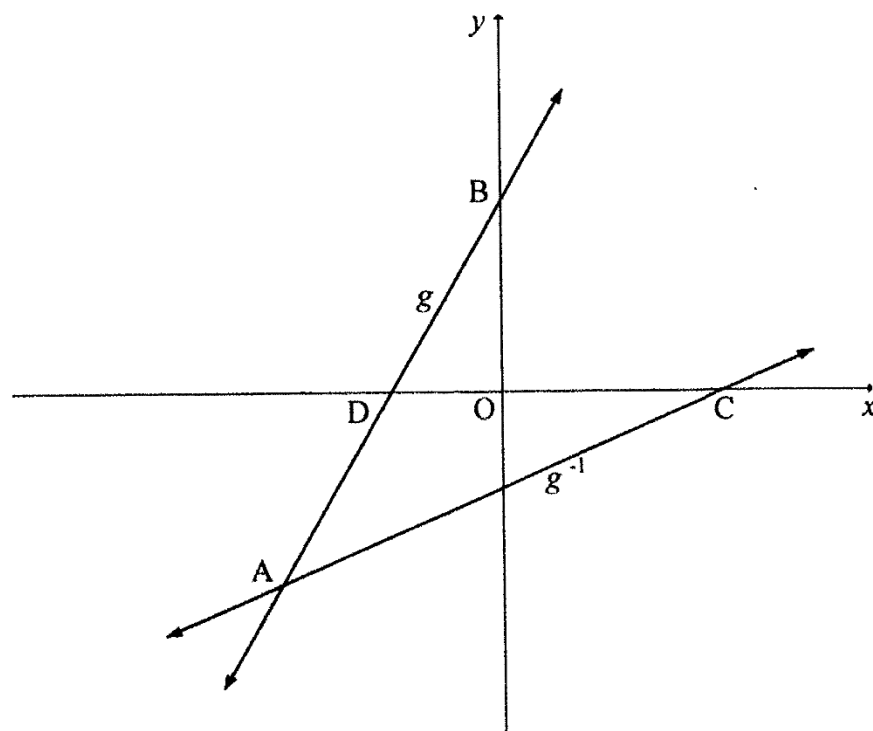
5.1	Write down the y-coordinate of B.	(1)
5.2	Determine the equation of g^{-1} in the form $g^{-1}(x) = mx + n$.	(2)
5.3	Determine the coordinates of A.	(3)
5.4	Calculate the length of AB.	(2)
5.5	Calculate the area of $\triangle ABC$.	(5)

[13]

QUESTION 6

6.1 R12 000 was invested in a fund that paid interest at m% p.a., compounded quarterly. After 24 months, the value of the investment was R13 459.

Determine the value of m. (4)

6.2 On 31 January 2022, Tino deposited R1 000 in an account that paid interest at 7,5% p.a., compounded monthly. He continued depositing R1 000 on the last day of every month. He will make the last deposit on 31 December 2022.

Will Tino have sufficient funds in the account on 1 January 2023 to buy a computer that costs R13 000? Justify your answer by means of an appropriate calculation. (4)

6.3 Thabo plans to buy a car that costs R250 000. He will pay a deposit of 15% and take out a loan for the balance. The interest on the loan is 13% p.a., compounded monthly.

6.3.1 Calculate the value of the loan. (1)

6.3.2 The first repayment will be made 6 months after the loan has been granted. The loan will be repaid over a period of 6 years after it has been granted. Calculate the MONTHLY instalment. (5)

[14]

QUESTION 7

7.1 Determine $f'(x)$ from first principles if $f(x) = x^2 + x$. (5)

7.2 Determine $f'(x)$ if $f(x) = 2x^5 - 3x^4 + 8x$. (3)

7.3 The tangent to $g(x) = ax^3 + 3x^2 + bx + c$ has a minimum gradient at the point $(-1 ; -7)$. For which values of x will g be concave up? (4)
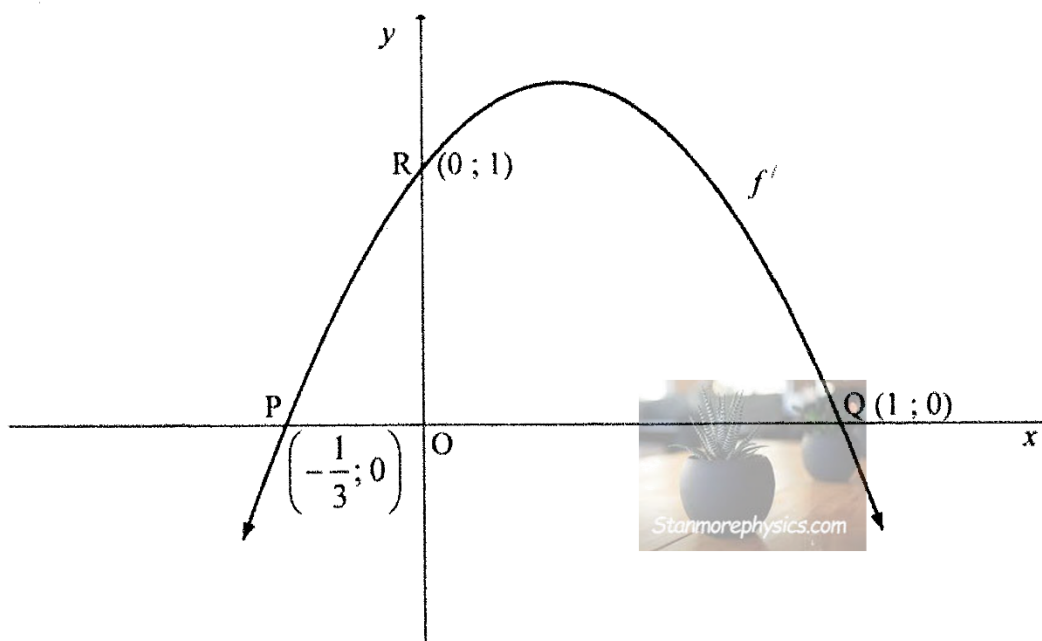
[12]

QUESTION 8

The graph of $y = f'(x) = mx^2 + nx + k$ is drawn below.

The graph passes the points $P\left(-\dfrac{1}{3}\,;\,0\right)$, $Q(1\,;\,0)$ and $R(0\,;\,1)$.

8.1 Determine the values of m, n and k. (6)

8.2 If it is further given that $f(x) = -x^3 + x^2 + x + 2$:

    8.2.1 Determine the coordinates of the turning points of f. (3)

    8.2.2 Draw the graph of f. Indicate on your graph the coordinates of the turning points and the intercepts with the axes. (5)

8.3 Points E and W are two variable points on f' and are on the same horizontal line.
- h is a tangent to f' at E.
- g is a tangent to f' at W.
- h and g intersect at $D(a\,;\,b)$.

    8.3.1 Write down the value of a. (1)

    8.3.2 Determine the value(s) of b for which h and g will no longer be tangents to f'. (2)
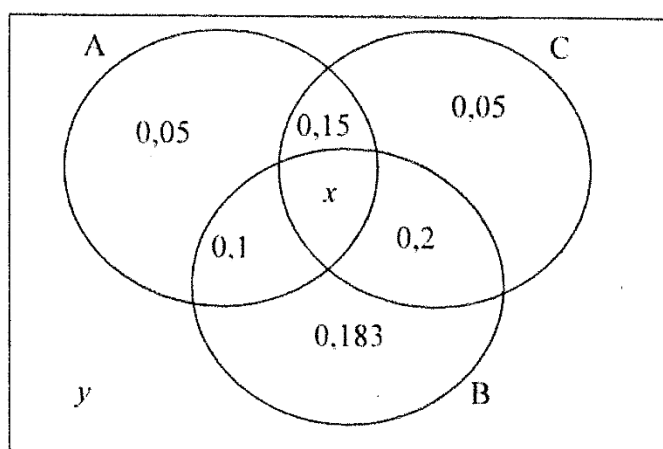
[17]

QUESTION 9

Given $f(x) = x^2$.

Determine the minimum distance between the point $(10 ; 2)$ and a point on f. [8]

QUESTION 10

10.1 A, B and C are three events. The probabilities of these events (or any combination of them) occurring is given in the Venn-diagram below

10.1.1 If it is given that the probability that at least one of the events will occur is 0,893, calculate the value of:

(a) y, the probability that none of the events will occur. (1)

(b) x, the probability that all three events will occur. (1)

10.1.2 Determine the probability that at least two of the events will take place. (2)

10.1.3 Are events B and C independent? Justify your answer. (5)

10.2 A four-digit code is required to open a combination lock. The code must be even-numbered and may not contain the digits 0 or 1. Digits may not be repeated.

10.2.1 How many possible 4-digit combinations are there to open the lock? (3)

10.2.2 Calculate the probability that you will open the lock at the first attempt if it is given that the code is greater than 5 000 and the third digit is 2. (5)

[17]

TOTAL: 150

INFORMATION SHEET

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni) \qquad A = P(1 - ni) \qquad A = P(1 - i)^n \qquad A = P(1 + i)^n$$

$$T_n = a + (n-1)d \qquad\qquad S_n = \frac{n}{2}\left[2a + (n-1)d\right]$$

$$T_n = ar^{n-1} \qquad\qquad S_n = \frac{a(r^n - 1)}{r - 1} \;;\; r \neq 1 \qquad S_\infty = \frac{a}{1 - r} \;;\; -1 < r < 1$$

$$F = \frac{x\left[(1 + i)^n - 1\right]}{i} \qquad\qquad P = \frac{x\left[1 - (1 + i)^{-n}\right]}{i}$$

$$f'(x) = \lim_{h \to 0} \frac{f(x + h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \qquad\qquad M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c \qquad\qquad y - y_1 = m(x - x_1) \qquad m = \frac{y_2 - y_1}{x_2 - x_1} \qquad m = \tan\theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \triangle ABC: \ \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc.\cos A$$

$$\text{area } \triangle ABC = \frac{1}{2}ab.\sin C$$

$$\sin(\alpha + \beta) = \sin\alpha.\cos\beta + \cos\alpha.\sin\beta \qquad \sin(\alpha - \beta) = \sin\alpha.\cos\beta - \cos\alpha.\sin\beta$$

$$\cos(\alpha + \beta) = \cos\alpha.\cos\beta - \sin\alpha.\sin\beta \qquad \cos(\alpha - \beta) = \cos\alpha.\cos\beta + \sin\alpha.\sin\beta$$

$$\cos 2\alpha = \begin{cases} \cos^2\alpha - \sin^2\alpha \\ 1 - 2\sin^2\alpha \\ 2\cos^2\alpha - 1 \end{cases} \qquad\qquad \sin 2\alpha = 2\sin\alpha.\cos\alpha$$

$$\bar{x} = \frac{\sum x}{n} \qquad\qquad \sigma^2 = \frac{\sum_{i=1}^{n}(x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)} \qquad\qquad P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx \qquad\qquad b = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sum(x - \bar{x})^2}$$

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**NATIONAL
SENIOR CERTIFICATE/
*NASIONALE SENIOR
SERTIFIKAAT***

GRADE 12/*GRAAD 12*

MATHEMATICS P1/*WISKUNDE V1*
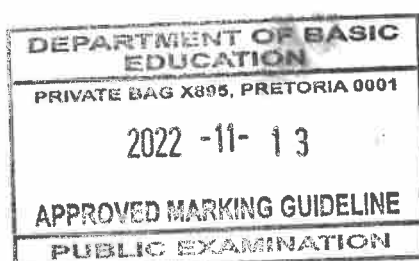
NOVEMBER 2022

MARKING GUIDELINES/*NASIENRIGLYNE*

MARKS/*PUNTE*: 150

These marking guidelines consist of 20 pages.
Hierdie nasienriglyne bestaan uit 20 bladsye.

DEPARTMENT OF BASIC
EDUCATION
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2022 -11- 1 3

APPROVED MARKING GUIDELINE
PUBLIC EXAMINATION

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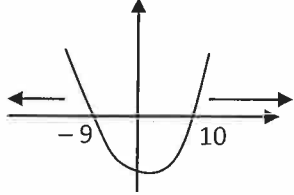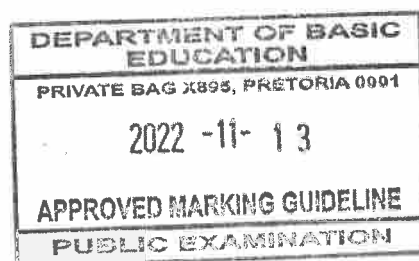Please turn over/*Blaai om asseblief*

NOTE:
- If a candidate answers a question TWICE, only mark the FIRST attempt.
- Consistent Accuracy applies in all aspects of the marking guidelines.

LET WEL:
- *Indien 'n kandidaat 'n vraag TWEE keer beantwoord, sien slegs die EERSTE poging na.*
- *Volgehoue akkuraatheid is DEURGAANS op ALLE aspekte van die nasienriglyne van toepassing.*

QUESTION1/*VRAAG* 1

1.1.1	$(3x-6)(x+2)=0$ $x=2$ or $x=-2$	✓ $x=2$ ✓ $x=-2$ (2)
1.1.2	$2x^2-6x+1=0$ $x=\dfrac{-b\pm\sqrt{b^2-4ac}}{2a}$ $x=\dfrac{6\pm\sqrt{(-6)^2-4(2)(1)}}{2(2)}$ $x=2{,}82$ or $x=0{,}18$	✓ correct substitution into correct formula ✓ 2,82 ✓ 0,18 (3)
1.1.3	$x^2-90>x$ $x^2-x-90>0$ $(x+9)(x-10)>0$ CV: $x=-9$ or $x=10$ $x<-9$ or $x>10$ **OR/OF** $(-\infty\,;-9)$ or $(10\,;\infty)$	✓ standard form ✓ critical values ✓✓ $x<-9$ or $x>10$ (4)

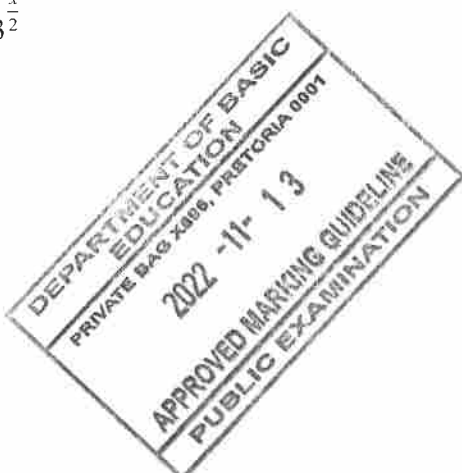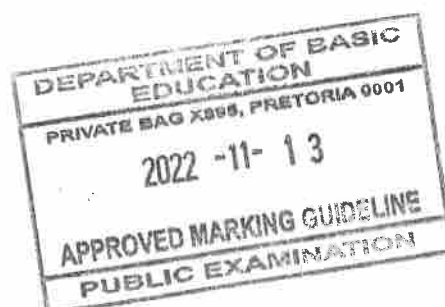|		
1.1.4	$x - 7\sqrt{x} = -12$ $x + 12 = 7\sqrt{x}$ $(x+12)^2 = \left(7\sqrt{x}\right)^2$ $x^2 + 24x + 144 = 49x$ $x^2 - 25x + 144 = 0$ $(x-16)(x-9) = 0$ $x = 16$ or $x = 9$ **OR/*OF*** $x - 7\sqrt{x} + 12 = 0$ $\left(\sqrt{x}-3\right)\left(\sqrt{x}-4\right) = 0$ or let $\sqrt{x} = k$ $\sqrt{x} = 3$ or $\sqrt{x} = 4$ $x = 9$ or $x = 16$	✓ isolating the root ✓ squaring both sides ✓ standard form ✓ both answers (4) **OR/*OF*** ✓ standard form ✓ factors ✓ answers ✓ both answers for x (4)
1.2	$2x - y = 2$ $y = 2x - 2$ ....(1) $xy = 4$ ....(2) (1) in (2): $x(2x-2) = 4$ $2x^2 - 2x - 4 = 0$ $x^2 - x - 2 = 0$ $(x-2)(x+1) = 0$ $x = 2$ or $x = -1$ $y = 2$ $y = -4$	✓ eq 1 ✓ substitution ✓ standard form ✓ x-values ✓ y-values (5)

OR/*OF* $2x - y = 2$ $x = \dfrac{1}{2}y + 1 \quad \ldots\ldots\ldots(1)$ $xy = 4 \quad \ldots\ldots\ldots(2)$ (1) in (2): $y\left(\dfrac{1}{2}y + 1\right) = 4$ $\dfrac{1}{2}y^2 + y - 4 = 0$ $y^2 + 2y - 8 = 0$ $(y + 4)(y - 2) = 0$ $y = -4 \quad$ or $\quad y = 2$ $x = -1 \qquad x = 2$	**OR/*OF*** ✓ eq 1 ✓ substitution ✓ standard form ✓ y-values ✓ x-values (5)
OR/OF $2x - y = 2 \quad \ldots\ldots\ldots(1)$ $y = \dfrac{4}{x} \quad \ldots\ldots\ldots(2)$ (2) in (1): $2x - \dfrac{4}{x} = 2$ $2x^2 - 2x - 4 = 0$ $x^2 - x - 2 = 0$ $(x - 2)(x + 1) = 0$ $x = 2 \quad$ or $\quad x = -1$ $y = 2 \qquad y = -4$	**OR/OF** ✓ eq 2 ✓ substitution ✓ standard form ✓ x-values ✓ y-values (5)

	OR/OF $2x - y = 2$ ………(1) $x = \dfrac{4}{y}$ ………(2) (2)in (1): $2\left(\dfrac{4}{y}\right) - y = 2$ $8 - y^2 - 2y = 0$ $y^2 + 2y - 8 = 0$ $(y+4)(y-2) = 0$ $y = -4$ or $y = 2$ $x = -1 \qquad x = 2$	**OR/OF** ✓ eq 2 ✓ substitution ✓ standard form ✓ y-values ✓ x-values $\qquad$ (5)
1.3	$2.5^n - 5^{n+1} + 5^{n+2} = 2.5^n - 5^n.5^1 + 5^n.5^2$ $\qquad\qquad = 5^n(2 - 5 + 25)$ $\qquad\qquad = 5^n(22)$ $2(5^n(11))$ **OR/OF** Any integer multiplied by an even number will be even	✓ exp law ✓common factor ✓answer/explanation $\quad$ (3)
1.4	$\dfrac{3^{y+1}}{32} = \sqrt{96^x}$ $\dfrac{3^{y+1}}{2^5} = (96)^{\frac{x}{2}}$ $3^{y+1}.2^{-5} = 2^{\frac{5x}{2}}.3^{\frac{x}{2}}$ $-5 = \dfrac{5x}{2}$ $\therefore x = -2$ $y + 1 = \dfrac{x}{2}$ $y + 1 = \dfrac{-2}{2}$ $\therefore y = -2$	✓ $\dfrac{3^{y+1}}{2^5} = (96)^{\frac{x}{2}}$ ✓ $3^{y+1}.2^{-5} = 2^{\frac{5x}{2}}.3^{\frac{x}{2}}$ ✓ $x = -2$ ✓ $y = -2$ $\qquad$ (4)

	OR/OF	**OR/OF**
	$\dfrac{3^{y+1}}{32} = \sqrt{96^x}$	
	$\left(\dfrac{3^{y+1}}{2^5}\right)^2 = \left(\sqrt{(96)^x}\right)^2$	$\checkmark$ $\left(\dfrac{3^{y+1}}{2^5}\right)^2 = \left(\sqrt{(96)^x}\right)^2$
	$\dfrac{3^{2y+2}}{2^{10}} = 2^{5x}.3^x$	
	$3^{2y+2}.2^{-10} = 2^{5x}.3^x$	$\checkmark$ $3^{2y+2}.2^{-10} = 2^{5x}.3^x$
	$-10 = 5x$	
	$\therefore x = -2$	$\checkmark$ $x = -2$
	$2y + 2 = -2$	
	$\therefore y = -2$	$\checkmark$ $y = -2$ (4)
		[25]

QUESTION 2/VRAAG 2

2.1.1	$a = 14$ $T_6 = 14r^5 = 448$ $\boxed{\text{Answer only: full marks}}$ $r^5 = 32$ $\therefore r = 2$	$\checkmark T_6 = 14r^5 = 448$ $\checkmark r = 2$ (2)
2.1.2	$T_n = 14(2)^{n-1}$ $S_n = \dfrac{14(2^6 - 1)}{2 - 1}$ $S_6 = 882$ $114\,674 - 882 = 113\,792$ $113\,792 = 896\left(2^n - 1\right)$ $128 = 2^n$ $n = 7$ **OR/OF** $S_n = \dfrac{a(r^n - 1)}{r - 1}$ $114\,674 = \dfrac{14(2^n - 1)}{2 - 1}$ $8\,191 = 2^n - 1$ $2^n = 8\,192$ $n = \log_2 8\,192$ $n = 13$ $\therefore$ 7 more terms must be added to the first 6 terms.	$\checkmark$ substitution into correct formula $\checkmark S_6 = 882$ $\checkmark 128 = 2^n$ $\checkmark 7$ (4) **OR/OF** $\checkmark$ substitution into correct formula $\checkmark 2^n = 8\,192$ $\checkmark n = 13$ $\checkmark 7$ (4)
2.1.3	$r = \dfrac{1}{2}$ $\qquad$ OR $\qquad 448r^5 = 14$ $\qquad\qquad\qquad\qquad \therefore r = \dfrac{1}{2}$ $S_\infty = \dfrac{a}{1 - r}$ $S_\infty = \dfrac{448}{1 - \dfrac{1}{2}}$ $S_\infty = 896$	$\checkmark r = \dfrac{1}{2}$ $\checkmark$ substitution $\checkmark$ answer (3)

2.2	$\sum_{p=0}^{k}\left(\frac{1}{3}p+\frac{1}{6}\right)=20\frac{1}{6}$	
	$T_1=\frac{1}{6} \qquad T_2=\frac{1}{3}+\frac{1}{6}=\frac{3}{6}$	$\checkmark\ T_1=\frac{1}{6}$
	$d=\frac{3}{6}-\frac{1}{6}=\frac{1}{3}$	$\checkmark\ d$
	$\frac{121}{6}=\frac{n}{2}\left[2\left(\frac{1}{6}\right)+(n-1)\left(\frac{1}{3}\right)\right]$	$\checkmark$ substitution
	$\frac{121}{3}=n\left[\frac{1}{3}+\frac{1}{3}n-\frac{1}{3}\right]$	
	$\frac{121}{3}=\frac{1}{3}n^2$	
	$121=n^2$	
	$n=11$	$\checkmark$ value of n
	$\therefore k=10$	$\checkmark$ value of k (5)
	OR/*OF*	**OR/*OF***
	$\sum_{p=0}^{k}\left(\frac{1}{3}p+\frac{1}{6}\right)=20\frac{1}{6}$	
	$a=\frac{1}{6}$	$\checkmark\ a=\frac{1}{6}$
	$l=\frac{1}{3}k+\frac{1}{6}$	$\checkmark\ l$
	$n=k+1$	$\checkmark\ n=k+1$
	$S_n=\frac{n}{2}[a+l]$	
	$\frac{121}{6}=\frac{k+1}{2}\left[\frac{1}{6}+\frac{1}{3}k+\frac{1}{6}\right]$	
	$\frac{121}{6}=\frac{k+1}{2}\left[\frac{1}{3}k+\frac{1}{3}\right]$	
	$\frac{121}{6}=\frac{k+1}{2}\left[\frac{k+1}{3}\right]$	
	$\frac{121}{6}=\frac{(k+1)^2}{6}$	$\checkmark\ \frac{121}{6}=\frac{(k+1)^2}{6}$
	$k+1=\pm\sqrt{121}$	
	$k+1=11$	
	$k=10$	$\checkmark$ value of k (5)
		[14]

QUESTION 3/*VRAAG 3*

3.1	$3a + b = 7$ $\quad 3 + b = 7$ $\qquad b = 4$ **OR/OF** $T_2 - T_1 = 7$ $4 + 2b + 9 - (1 + b + 9) = 7$ $b = 4$	$\checkmark$ $3a + b = 7$ $\checkmark$ $3 + b = 7$ (2) **OR/OF** $\checkmark$ $T_2 - T_1 = 7$ $\checkmark$ substitution (2)
3.2	$T_n = n^2 + 4n + 9$ $T_{60} = (60)^2 + 4(60) + 9$ $\boxed{\text{Answer only: full marks}}$ $\quad = 3849$	$\checkmark$ substitution $\checkmark$ answer (2)
3.3	$14 \; ; \; 21 \; ; \; 30 \; ; \; 41;$ First difference: $7 \; ; \; 9 \; ; \; 11 \; ; \; \dots$ Common 2nd difference: 2 $T_p = 2p + 5$ $\boxed{\text{Answer only: full marks}}$ **OR/*OF*** First difference: $7 \; ; \; 9 \; ; \; 11 \; ; \; \dots$ $T_n = a + (n-1)d$ $\quad T_p = 7 + (p-1)(2)$ $\quad T_p = 2p + 5$	$\checkmark$ first difference $\checkmark$ 2 $\checkmark$ $2p + 5$ (3) **OR/*OF*** $\checkmark$ first difference $\checkmark$ 2 $\checkmark$ $2p + 5$ (3)
3.4	$157 = 2p + 5$ $p = 76$ $\therefore$ Between T_{76} and T_{77} **OR/OF** $\qquad\qquad T_{n+1} - T_n = 157$ $(n+1)^2 + 4(n+1) + 9 - (n^2 + 4n + 9) = 157$ $n^2 + 2n + 1 + 4n + 4 + 9 - n^2 - 4n - 9 = 157$ $\qquad\qquad\qquad 2n = 152$ $\qquad\qquad\qquad n = 76$ $\therefore$ Between T_{76} and T_{77}	$\checkmark$ $157 = 2p + 5$ $\checkmark$ $p = 76$ $\checkmark$ T_{76} and T_{77} (3) **OR/OF** $\checkmark$ $T_{n+1} - T_n = 157$ $\checkmark$ $n = 76$ $\checkmark$ T_{76} and T_{77} (3)
		[10]

QUESTION 4/*VRAAG* 4

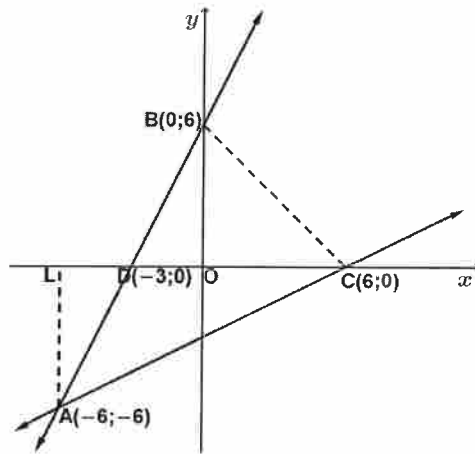|		
4.1.1	$p = -1$ and $q = 2$	✓ $p = -1$ ✓ $q = 2$ (2)
4.1.2	$\dfrac{1}{x-1} + 2 = 0$ $-2x + 2 = 1$ $x = \dfrac{1}{2}$ $\left(\dfrac{1}{2}\ ;\ 0\right)$	✓ $= 0$ ✓ answer (2)
4.1.3	$x = \dfrac{1}{2} - 3$ $= \dfrac{-5}{2}$ Answer only: full marks	✓ -3 ✓ $x = \dfrac{-5}{2}$ (2)
4.1.4	$y = x + t$ $2 = 1 + t$ $t = 1$	✓ subst $(1\ ;\ 2)$ ✓ $t = 1$ (2)
4.1.5	$-2 \leq \dfrac{1}{x-1}$ Answer only: full marks $\dfrac{1}{x-1} + 2 \geq 0$ $\therefore x \leq \dfrac{1}{2}$ or $x > 1$ **OR/*OF*** $x \in \left(-\infty\ ;\ \dfrac{1}{2}\right]$ or $(1\ ;\ \infty)$	 ✓ $\dfrac{1}{x-1} + 2 \geq 0$ ✓ $x \leq \dfrac{1}{2}$ ✓ $x > 1$ (3)
4.2.1	$y = -5$	✓ answer (1)
4.2.2	$x = \dfrac{-b}{2a} = \dfrac{-(-4)}{2(1)} = 2$ $f(2) = 2^2 - 4(2) - 5 = -9$ $\therefore \text{D}(2\ ;\ -9\ )$ **OR/*OF*** $f'(x) = 2x - 4$ $2x - 4 = 0$ $x = 2$ $f(2) = 2^2 - 4(2) - 5 = -9$ $\therefore \text{D}(2\ ;\ -9\ )$	✓ $x = 2$ ✓ $y = -9$ (2) **OR/*OF*** ✓ $x = 2$ ✓ $y = -9$ (2)

4.2.3	$q = -5$	$\checkmark\ q = -5$	
	$-9 = a(2)^2 - 5$	$\checkmark$ substitution of $(2\ ;-9)$	
	$-4 = 4a$		
	$a = -1$	$\checkmark\ a = -1$	
	$\therefore g(x) = -2^x - 5$		(3)
4.2.4	$y \in (-\infty\ ;-5)$ OR $y < -5; y \in R$	$\checkmark$ answer	(1)
4.2.5	$k < -9$	$\checkmark -9$	
		$\checkmark\ k < -9$	(2)
			[20]

QUESTION 5/*VRAAG* 5

5.1	$g(x) = 2x + 6$ $y = 6$		$\checkmark\, y = 6$	(1)
5.2	$y = 2x + 6$ $x = 2y + 6$ $y = \dfrac{1}{2}x - 3$	Answer only: Full marks	$\checkmark$ swop x and y $\checkmark$ equation	(2)
5.3	$\dfrac{1}{2}x - 3 = 2x + 6$ $x - 6 = 4x + 12$ $3x = -18$ $x = -6$ A$(-6\,;-6)$ **OR/*OF*** $2x + 6 = x$ $x = -6$ $y = -6$		$\checkmark$ equating $\checkmark\, x = -6$ $\checkmark\, y = -6$ (3) **OR/*OF*** $\checkmark$ equating $\checkmark\, x = -6$ $\checkmark\, y = -6$ (3)	
5.4	$AB = \sqrt{(6)^2 + (12)^2}$ $\quad = \sqrt{180} = 6\sqrt{5} = 13{,}42$		$\checkmark$ substitution $\checkmark$ answer	(2)

5.5	$BC = \sqrt{6^2 + 6^2} = \sqrt{72} = 6\sqrt{2}$	✓ BC
	$AB = AC = \sqrt{180}$ symmetry of g and g^{-1}	✓ AB = AC /midpoint (3 ; 3)
	$\perp h = (\sqrt{180})^2 - \left(\dfrac{\sqrt{72}}{2}\right)^2$	✓ $\perp h$ (A)
	$\qquad = \sqrt{162} = 9\sqrt{2}$	
	area of $\triangle ABC = \dfrac{1}{2} BC \times h$	✓ substitution
	$\qquad = \dfrac{1}{2} \times \sqrt{72} \times \sqrt{162} = 54 \text{ units}^2$	✓ answer (A) (5)
	OR/*OF*	**OR/*OF***
	$\tan B\hat{D}C = 2$	
	$\therefore B\hat{D}C = 63{,}43°$	✓ $B\hat{D}C = 63{,}43°$
	$\tan D\hat{C}A = \dfrac{1}{2}$	
	$\therefore D\hat{C}A = 26{,}57°$	
	$\therefore D\hat{A}C = 36{,}86°$ (ext angle triangle)	✓ $D\hat{A}C = 36{,}86°$
		✓ AC = $\sqrt{180}$
	Area of $\triangle ABC = \dfrac{1}{2}\left(\sqrt{180}\right)\left(\sqrt{180}\right)\sin 36{,}86°$	✓ substitution into the correct formula
	$\qquad = 53{,}99 \text{ units}^2$	✓ answer (A) (5)
	OR/OF	**OR/OF**
	Area of $\triangle ABC$ = Area of $\triangle BDC$ + Area of $\triangle ADC$	✓ Areas ($\triangle BDC + \triangle ADC$)
	$\qquad = \dfrac{1}{2} DC.BO + \dfrac{1}{2} DC.height$	✓ $\dfrac{1}{2} DC.BO$
	$\qquad = \dfrac{1}{2}(9)(6) + \dfrac{1}{2}(9)(6)$	✓ $\dfrac{1}{2} DC.height$
	$\qquad = 54 \text{ units}^2$	✓ substitution
		✓ answer (A) (5)
		[13]

QUESTION 6/VRAAG 6

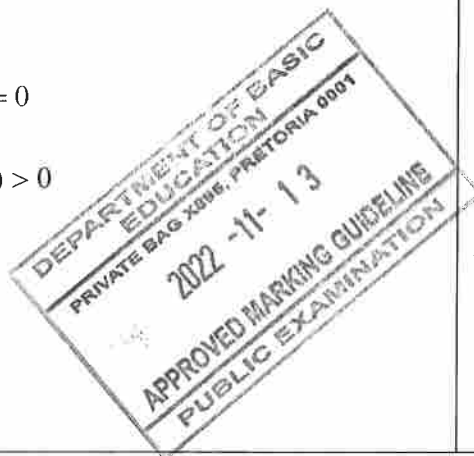|		
6.1	$A = P(1+i)^n$ $13\,459 = 12\,000\left(1+\dfrac{m}{400}\right)^8$ $\left(1+\dfrac{m}{400}\right)^8 = 1,121...$ $1+\dfrac{m}{400} = \sqrt[8]{1,121..}$ $\dfrac{m}{400} = 0,0144...$ $\therefore m = 5,78\%$	✓ 8 ✓ subst into correct formula ✓ $1+\dfrac{m}{400} = \sqrt[8]{1,121..}$ ✓ 5,78 % (4)
6.2	$F = \dfrac{x\left[(1+i)^n - 1\right]}{i}$ $F = \dfrac{1\,000\left[\left(1+\dfrac{0,075}{12}\right)^{12} - 1\right]}{\dfrac{0,075}{12}}$ $= R12\,421,22$ He won't be able to buy the computer because R13 000 – R12 421,22 = R578,78 **OR/OF** He won't be able to buy the computer because R12 421,22 < R13 000	✓ $\dfrac{0,075}{12}$ ✓ 12 ✓ answer ✓ conclusion (4)
6.3.1	Loan amount = 85% × R250 000 = R212 500 **OR/OF** Loan amount = R250 000 – (15% × R250 000) = R212 500	✓ answer (1) **OR/OF** ✓ answer (1)
6.3.2	$A = 212\,500\left(1+\dfrac{0,13}{12}\right)^5$ $A = 224\,262,53$ $P = \dfrac{x\left[1-(1+i)^{-n}\right]}{i}$ $224\,262,53 = \dfrac{x\left[1-\left(1+\dfrac{0,13}{12}\right)^{-67}\right]}{\dfrac{0,13}{12}}$ $\therefore x = R4\,724,96$	✓ $A = 212\,500\left(1+\dfrac{0,13}{12}\right)^5$ ✓ answer ✓ substitution into correct formula ✓ – 67 ✓ answer (5)
		[14]
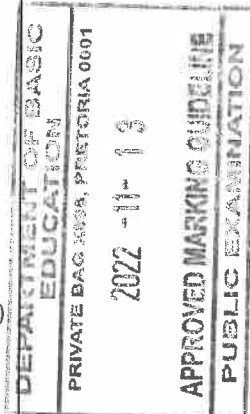
QUESTION 7/*VRAAG* 7
Notation penalty only in Question 7.1

7.1	$f(x) = x^2 + x$	
	$f'(x) = \lim_{h \to 0} \dfrac{f(x+h) - f(x)}{h}$	
	$f'(x) = \lim_{h \to 0} \dfrac{(x+h)^2 + (x+h) - (x^2 + x)}{h}$	✓substitution into the formula
	$f'(x) = \lim_{h \to 0} \dfrac{x^2 + 2xh + h^2 + x + h - x^2 - x}{h}$	✓ $x^2 + 2xh + h^2 + x + h$
	$= \lim_{h \to 0} \dfrac{2xh + h^2 + h}{h}$	✓ $2xh + h^2 + h$
	$= \lim_{h \to 0} \dfrac{h(2x + h + 1)}{h}$	✓common factor
	$\therefore f'(x) = 2x + 1$	✓answer (5)
	OR/*OF*	**OR/*OF***
	$f(x) = x^2 + x$	
	$f(x+h) = (x+h)^2 + (x+h) = x^2 + 2xh + h^2 + x + h$	✓ $x^2 + 2xh + h^2 + x + h$
	$f(x+h) - f(x) = x^2 + 2xh + h^2 + x + h - x^2 - x$	
	$\qquad\qquad = 2xh + h^2 + h$	✓ $2xh + h^2 + h$
	$f'(x) = \lim_{h \to 0} \dfrac{f(x+h) - f(x)}{h}$	
	$= \lim_{h \to 0} \dfrac{2xh + h^2 + h}{h}$	✓substitution into the formula
	$= \lim_{h \to 0} \dfrac{h(2x + h + 1)}{h}$	✓common factor
	$\therefore f'(x) = 2x + 1$	✓answer (5)
7.2	$f(x) = 2x^5 - 3x^4 + 8x$	✓ $10x^4$
	$f'(x) = 10x^4 - 12x^3 + 8$	✓ $-12x^3$
		✓ 8 (3)
7.3	$g(x) = ax^3 + 3x^2 + bx + c$	
	$g'(x) = 3ax^2 + 6x + b$	✓ $g'(x) = 3ax^2 + 6x + b$
	$g''(x) = 6ax + 6$	✓
	$g''(-1) = 6a(-1) + 6 = 0$	✓ $g''(-1) = 6a(-1) + 6 = 0$
	$\therefore a = 1$	✓ $a = 1$
	For concave up $g''(x) > 0$	
	$6x + 6 > 0$	
	$x > -1$	✓ $x > -1$ (4)
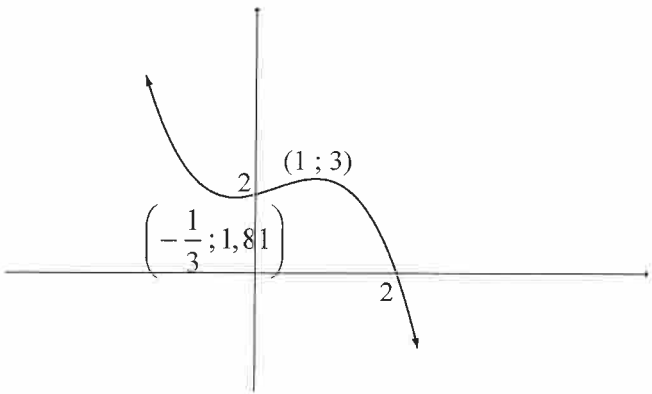
OR/OF

Min gradient at $(-1 ; -7)$ implies:

at $x = -1$ - point of inflection
and g will be positive cubic
hence $a > 0$

Since g is concave up

$x > -1$

OR/OF

$(-1 ; -7)$

Since g is concave up
$x > -1$

$(-1 ; y)$

Since g is concave up
$x > -1$

Answer only: $\dfrac{1}{4}$

OR/OF

✓ point of inflection

✓✓ $a > 0$

✓ $x > -1$ (4)

OR/OF

✓✓ pos graph

✓ point of inflection

✓ $x > -1$ (4)

[12]

QUESTION 8/*VRAAG* 8
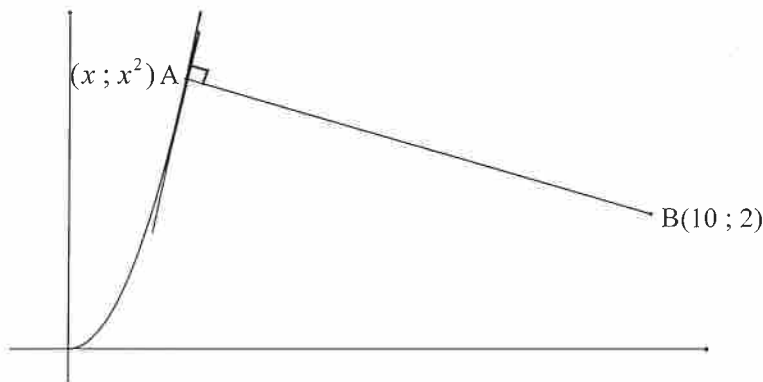
8.1	$f'(x) = mx^2 + nx + k$ $$f'(x) = m\left(x + \frac{1}{3}\right)(x-1)$$ $$1 = m\left(0 + \frac{1}{3}\right)(0-1)$$ $$1 = -\frac{1}{3}m$$ $$\therefore m = -3$$ $$f'(x) = -3\left(x + \frac{1}{3}\right)(x-1)$$ $$f'(x) = -3\left(x^2 - \frac{2}{3}x - \frac{1}{3}\right)$$ $$f'(x) = -3x^2 + 2x + 1$$ $$\therefore n = 2$$ $$\therefore k = 1$$ **OR/OF** $$k = 1$$ $$0 = m + n + 1 \quad \text{and} \quad \frac{1}{9}m - \frac{1}{3}n + 1 = 0$$ $$m + n = -1 \qquad (1)$$ $$m - 3n = -9 \qquad (2)$$ $$(1) - (2)$$ $$4n = 8$$ $$\therefore n = 2$$ $$m + 2 = -1$$ $$\therefore m = -3$$	✓ substitution of $\left(-\frac{1}{3} ; 0\right)$ and $(1 ; 0)$ ✓ substitution of $(0 ; 1)$ ✓ $m = -3$ ✓ $f'(x) = -3\left(x^2 - \frac{2}{3}x - \frac{1}{3}\right)$ ✓ $n = 2$ ✓ $k = 1$ (6) **OR/OF** ✓ $k = 1$ ✓ $m + n = -1$ ✓ $m - 3n = -9$ ✓ $4n = 8$ ✓ $n = 2$ ✓ $m = -3$ (6)
8.2.1	$f(x) = -x^3 + x^2 + x + 2$ $$f\left(-\frac{1}{3}\right) = \frac{49}{27} = 1{,}81$$ $$\text{T.P}\left(-\frac{1}{3} ; \frac{49}{27}\right)$$ $$f(1) = 3$$ $$\text{T.P}(1 ; 3)$$	✓ x-coordinates of the TP ✓ T.P$\left(-\frac{1}{3} ; \frac{49}{27}\right)$ ✓ T.P$(1 ; 3)$ (3)

8.2.2	$f(x) = -x^3 + x^2 + x + 2$	
	$-x^3 + x^2 + x + 2 = 0$	
	$(x-2)(-x^2 - x - 1) = 0$	
	$x = 2$ or no solution	✓ $x = 2$
		✓ one x-intercept
		✓ two turning points
		✓ y-intercept
		✓ shape: neg cubic
		(5)
8.3.1	$a = \dfrac{-\dfrac{1}{3} + 1}{2}$	
	$= \dfrac{1}{3}$	✓ answer (1)
	OR/OF	**OR/OF**
	$f'(x) = -3x^2 + 2x + 1$	
	$f''(x) = -6x + 2$	
	$f''(a) = -6a + 2 = 0$	
	$-6a = -2$	
	$a = \dfrac{1}{3}$	✓ answer (1)
8.3.2	$b < \dfrac{4}{3}$ units	✓ $\dfrac{4}{3}$
		✓ $b < \dfrac{4}{3}$ (2)
		[17]

QUESTION9/VRAAG 9

9.1	Any point on f : $(x\,;\,x^2)$	$\checkmark (x\,;\,x^2)$
	distance $= \sqrt{(x-10)^2 + (x^2-2)^2}$	$\checkmark$ substitution
	$\qquad = \sqrt{x^2 - 20x + 100 + x^4 - 4x^2 + 4}$	$\checkmark$ simplification
	$\qquad = \sqrt{x^4 - 3x^2 - 20x + 104}$	$\checkmark$ answer
	For min distance	
	$\dfrac{d}{dx}\left(x^4 - 3x^2 - 20x + 104\right) = 0$	
	$4x^3 - 6x - 20 = 0$	$\checkmark 4x^3 - 6x - 20$
	$(x-2)(4x^2 + 8x + 10) = 0$	$\checkmark$ derivative $= 0$
	$\qquad\quad \Delta = 8^2 - 4(4)(10) = -96 \quad \therefore$ no roots	
	$\therefore x = 2$	$\checkmark x = 2$
	$d = \sqrt{2^4 - 3(2)^2 - 20(2) + 104} = 2\sqrt{17} = 8{,}25$	$\checkmark$ answer (A) (8)

9.2	$m_{AB} = \dfrac{y_2 - y_1}{x_2 - x_1} = \dfrac{x^2 - 2}{x - 10}$	$\checkmark m_{AB}$
	$\therefore m_{\tan g} = -\dfrac{x-10}{x^2-2}$	$\checkmark m_{\tan g} = -\dfrac{x-10}{x^2-2}$
	$f'(x) = 2x$	$\checkmark f'(x) = 2x$
	$\therefore 2x = -\dfrac{x-10}{x^2-2}$	$\checkmark$ equating
	$-2x^3 + 4x = x - 10$	
	$2x^3 - 3x - 10 = 0$	$\checkmark$ standard form
	$x = 2$	$\checkmark x = 2$
	$y = (2)^2 = 4$	
	$\therefore AB = \sqrt{(2-10)^2 + (4-2)^2}$	$\checkmark$ substitute into distance
	$\qquad = 2\sqrt{17} = 8{,}25$	$\checkmark$ answer (A) (8)
		[8]

QUESTION 10/*VRAAG* 10

10.1.1(a)	$y = 1 - 0,893 = 0,107 \ (0,11)$	✓ $y = 1 - 0,893$ (1)
10.1.1(b)	$x = 0,893 - 0,733$ $\quad = 0,16$	✓ $x = 0,893 - 0,733$ (1)
10.1.2	P(at least 2 events) $= 0,1 + 0,15 + 0,16 + 0,2$ $\qquad\qquad\qquad\quad = 0,61$ Answer only: Full Marks	✓ values ✓ answer (2)
10.1.3	$P(B) = 0,643$ $P(C) = 0,56$ $P(B \text{ and } C) = 0,36$ $P(B) \times P(C) = 0,643 \times 0,56 = 0,36$ $\therefore P(B \text{ and } C) = P(B) \times P(C)$ $\therefore B$ and C are independent	✓ $P(B) = 0,643$ ✓ $P(C) = 0,56$ ✓ $P(B \text{ and } C) = 0,36$ ✓ $P(B) \times P(C) = 0,36$ ✓ independent because $\quad P(B \text{ and } C) = P(B) \times P(C)$ (5)
10.2.1	$7 \times 6 \times 5 \times 4 = 840$	✓ 4 ✓ 7 ✓ $7 \times 6 \times 5 \times 4 = 840$ (3)
10.2.2	start with 5, 7, 9 or start with 6 or start with 8 $(3 \times 5 \times 1 \times 3) + (1 \times 5 \times 1 \times 2) + (1 \times 5 \times 1 \times 2)$ $= 45 + 10 + 10$ $= 65$ $P = \dfrac{65}{840} = \dfrac{13}{168} = 0,08$ **OR/*OF*** ends in 4 or ends in 6 or ends in 8 $(5 \times 5 \times 1 \times 1) + (4 \times 5 \times 1 \times 1) + (4 \times 5 \times 1 \times 1)$ $= 25 + 20 + 20$ $= 65$ $P = \dfrac{65}{840} = \dfrac{13}{168} = 0,08$	✓ $(3 \times 5 \times 1 \times 3) = 45$ ✓ $(1 \times 5 \times 1 \times 2) = 10$ ✓ $(1 \times 5 \times 1 \times 2) = 10$ ✓ 65 ✓ answer (5) **OR/*OF*** ✓ $(5 \times 5 \times 1 \times 1) = 25$ ✓ $(4 \times 5 \times 1 \times 1) = 20$ ✓ $(4 \times 5 \times 1 \times 1) = 20$ ✓ 65 ✓ answer (5)
		[17]

TOTAL/*TOTAAL*: 150